ACCELERATED MATH GRADE 7: 180 Day Course	STATE STANDARD AREA/UNIT:	Algebraic Concepts: Expressions and Equations	TIME FRAME:	Ongoing
 NATIONAL COMMON CORE STAND Work the radicals and integer exp 8.EE.1 Know and apply the expressions. For example, . 8.EE.2 Use square root and and x³ = p, where p is a particular and cube roots of small periods 8.EE.3 Use numbers expressions. For example, estimate the as 7 x 10°, and determined 8.EE.4 Perform operations both decimal and scientific appropriate size for measure year for seafloor spreading Understand the connections betw 8.EE.5 Graph proportional Compare two different pro- compare a distance-time objects has greater speed 8.EE.6 Use similar triangles on a non-vertical line in th origin and the equation y Analyze and solve linear equation a. Give examples of I or no solutions. Sho given equation into a=b results (where b. Solve linear equation a. Give and solve particular a. Understand that solve particular 	ponents. e properties of integer exponents $3^2 \times 3^{-5} = 3^{-3} = 1/3^3 = 1/27$. d cube root symbols to represent ositive rational number. Evaluation erfect cubes. Know the √2 is irrect sed in the form of a single digit pantities, and to express how may population of the United State that the world population is more with numbers expressed in scient is notation are used. Use scient prements of very large or very sing). Interpret scientific notation the populational relationships, interpreting the up oportional relationships represent graph to a distance-time equal to explain why the slope m is the e coordinate plane; derive the = mx + b for a line intercepting the and pairs of simultaneous line possibilities is to possibilities is to possibilities of these possibilities is to possible forms, unit an equivale a and b are different numbers) ons with rational number coefficients expressions using the distributive possibilities to a system of two linear	ts to generate equivalent numerical at solutions to equations of the form $x^2 = p$ the square roots of small perfect squares ational. times an integer power of 10 to estimate any times as much one if than the other. as 3 x 10 ⁸ and the population of the world re than 20 times larger. Inific notation, including problems where ific notation and choose units of nall quantities (e.g., use millimeters per hat has been generated by technology. lines, and linear equations. nit rate as the slope of the graph. Inted in different ways. For example, tion to determine which of two moving the same between any two distinct points equation $y = mx$ for a line through the the vertical axis at b. ear equations. (Optional) with one solution, infinitely many solutions, the case by successively transforming the ent equation of the form $x = a$, $a = a$, or cients, including equations whose solutions e property and collecting like terms.	and per them. 2. Reason quantit 3. Constru- argume reason 4. Model 5. Use ap strateg 6. Attend 7. Look for structur 8. Look for	ense of problems ersevere in solving a abstractly and ratively uct viable ents and critique the ing of others. with mathematics. propriate tools ically. to precision. or and make use of re. or and express ity in repeated

	Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, $3x + 2y = 5$ and $3x + 2y = 6$ have no solution because $3x + 2y$ cannot simultaneously be 5 and 6.	
c.	Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of pints, determine whether the line through the first pair of points intersects the line through the second pair.	

ESSENTIAL QUESTIONS	VO	CABULARY	ASSESSMENT
 How do you work with radicals and integer exponents? What are the connections between proportional relationships, lines, and linear equations? How do you analyze and solve linear equations and pairs of simultaneous linear equations? (Optional) 	 radicals square roots cube roots scientific notation perfect square perfect cube proportional relationships 	 slope slope-intercept form similar figures unit rate linear equation systems of linear equations coefficient like terms 	Formative:• Journals/logs• KWL chart• At the bell activities• Question and answer• Thumbs up/thumbs down• Individual white boards/Promethean Board ActiVotes• Homework• Quizzes• Constructed response/open-ended problem solving• Performance tasks• Exit slipsSummative:• Benchmark assessments• Performance based assessments• Quizzes• Constructed response/open- ended problem solving• Performance based assessments• Constructed response/open- ended problem solving• Performance tasks• Spiral Review • Studylsland Practice

	PA CORE ASSESSMENT ANCHORS	PA ELIGIBLE CONTENT STANDARDS/ESSENTIAL CONTENT LEARNING ACTIVITIES
	CC.2.2.8.B.1: Apply concepts of radical and integer exponents to generate equivalent expressions.	M08.B-E.1: Represent and use expressions and equations to solve problems involving radicals and integer exponents.
EXPRESSIONS AND EQUATIONS	 Essential Skills and Understanding Ability to recognize and apply the following properties of integer exponents to generate equivalent numerical expressions without a calculator: Product/Quotient of Powers Negative Exponents Zero Exponents Power of Powers Ability to apply a combination of properties to show equivalency. Ability to recognize and apply the following: Perfect Squares Square Roots(Symbol Notation) Principal (positive) roots/negative roots Ability to recognize and of cubes with cube roots to represent and solve equations. Ability to compare large and small numbers using properties of integer exponents. Ability to read scientific notation on a calculator. CC.2.2.8.B.2: Understand the connections between proportional relationships, lines, and linear equations. 	 M08.B-E.1.1.1 Apply one or more properties of integer exponents to generate equivalent numerical expressions without a calculator (with final answers expressed in exponential form with positive exponents). M08.B-E.1.1.2 Use square root and cube root symbols to represent solutions to equations of the form x² = p and x³ = p, where p is a positive rational number. Evaluate square roots of perfect squares (up to and including 12²) and cube roots of perfect cubes (up to and including 5³) without a calculator. M08.B-E.1.1.3 Estimate very large or very small quantities by using numbers expressed in the form of a single digit times an integer power of 10 and express how many times larger or smaller one number is than another. M08.B-E.1.1.4 Perform operations with numbers expressed in scientific notation, including problems where both decimal and scientific notation are used. Express answers in scientific notation and choose units of appropriate size for measurements of very large or very small quantities (e.g., use millimeters per year for seafloor spreading). Interpret scientific notation that has been generated by technology (e.g., interpret 4.7EE9 displayed on a calculator as 4.7 x 10⁹).
	 Essential Skills and Understanding Ability to relate and compare graphic, symbolic, numerical representations of proportional relationships. Ability to calculate constant rate of change/slope of a line graphically. Ability to understand that all proportional relationships start at the origin. Ability to recognize and apply direct variation. Ability to understand that similar right triangles (provide diagram of graphical notation) can be used to establish that slope is constant for a non-vertical line. 	 M87.B-E.2: Understand the connections between proportional relationships, lines and linear equations. M08.B-E.2.1.1 Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. M08.B-E.2.1.2 Use similar right triangles to show and explain why the slope

UNIT OF INSTRUCTION:

	PA CORE ASSESSMENT ANCHORS	PA ELIGIBLE CONTENT STANDARDS/ESSENTIAL CONTENT LEARNING ACTIVITIES
	 Ability to graphically derive equations y = mx and y = mx + b. Ability to differentiate between zero slope and undefined slope. Ability to understand how the y-intercept translates a line along the y-axis (families of graphs). 	 <i>m</i> is the same between any two distinct points on a non-vertical line in the coordinate plane. M08.B-E.2.1.3 Derive the equation y = mx for a line through the origin and the equation y = mx + b for a line intercepting the vertical axis at b.
	CC.2.2.8.B.3: Analyze and solve linear equations and pairs of simultaneous linear equations.	M08.B-E.3: Analyze and solve linear equations and pairs of simultaneous linear equations.
EXPRESSIONS AND EQUATIONS	 Essential Skills and Understanding Ability to build on prior knowledge of solving linear equations. Ability to solve linear equations with rational number coefficient, including equations whose solutions require expanding expressions using the distributive property and combining like terms. Ability to solve simple cases by inspection, one solution, infinitely many solutions, or no solutions. Ability to write an equation given two points. Ability to write equations from context. Ability to interpret the solution to a system of equations in context. (Optional) Ability to solve systems of equations numerically or by graphing. (Optional) Ability to solve systems of two linear equations in two variables algebraically using substitution or elimination. (Optional) Ability to discuss efficient solution methods with a system of equations – graphically and algebraically. (Optional) 	 M08.B-E.3.1.1 Write and identify linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms until an equivalent equation of the form x = a, a = a, or a = b results (where a and b are different numbers). M08.B-E.3.1.2 Solve linear equations that have rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms. M08.B-E.3.1.3 (Optional) Interpret solutions to a system of two linear equations in two variables as points of intersection of their graphs because points of intersection satisfy both equations simultaneously. M08.B-E.3.1.4 (Optional) Solve systems of two linear equations in two variables algebraically and estimate solutions by graphing the equations. Solve simple cases by inspection. M08.B-E.3.1.5 (Optional) Solve real-world and mathematical problems leading to two linear equations in two variables.

UNITE OF INSTRUCTION:

	DIFFERENTIATION AC Teacher directed differentiated instructional projects and ac		
ENRICHMENT:	 Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials StudyIsland Ck12Math Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student 	REMEDIATION:	 Pearson Successnet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments Chunking of content, assignment and/or assessments One-on-one re-teaching Volunteer/peer tutoring Accommodations based on IEP and/or need ELL student (or based on student need) additional support Provide specific examples Simplified language in word problems Visuals Flashcards Multiple-meaning words Bilingual dictionary/picture dictionary

- Pre-Algebra, Pearson Education: Unit 1, 3, 4, 5, 7, 8, 11
- Grade 7 Unit: Algebraic Concepts: Expressions and Equations, as needed for review of new concepts
- StudyIsland, Ck12Math, other resources below: Expressions and Equations
- PDE SAS portal: <u>http://www.pdesas.org</u>
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - Click on the link to the PMSD ESEL Handbook
 - Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Grade 8 released state sample questions
- Grade 8 generated sample questions
- Promethean Flipcharts/ActiVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- http://www.khanacademy.org/
- Thinkfinity website: <u>http://www.thinkfinity.org/home</u>
- IXL Website: http://www.IXL.com/math/
- United Streaming: <u>http://streaming.discoveryeducation.com/index.cfm</u>
- <u>http://edhelper.com/place_value.html</u>
- <u>http://illuminations.nctm.org</u>
- <u>http://insidemathematics.org</u>
- <u>www.teachingchannel.org</u>
- <u>http://illustrativemathematics.org/standards/k8</u>
- <u>http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/</u>
- <u>www.teachingchannel.org</u>
- http://www.learnzillion.com
- <u>http://www.teacherspayteachers.com</u>
- <u>flexmath.ck12.org/</u>

ACCELERATED MATH GRADE 7: 180 Day Course	STATE STANDARD AREA/UNIT:	Algebraic Concepts: Functions	TIME FRAME:	Ongoing
 function is the set of order 8.F.2 Compare properties graphically, numerically is represented by a table of determine which function 8.F.3 Interpret the equation examples of functions that a function of its side lengs are not a on a straight line Use functions to model relationsthematics and initial value including reading these for linear function in terms of 8.F.5 Describe qualitative (e.g., where the function) 	functions. function is a rule that assigns to e ered pairs consisting of an input a es of two functions each represer in tables, or by verbal description of values and a linear function rep in has the greater rate of change ion $y = mx + b$ as defining a linear at are not linear. For example, the th is not linear because its graph the. hips between quantities. In to model a linear relationship b of the function from a description from a table or from a graph. In f the situation it models and in ter ely the functional relationship between the functional relationship between at a stable or from a graph.	nted in a different way (algebraically, hs). For example, given a linear function presented by an algebraic expression, ar function, whose graph is a straight line; give the function $A = s^2$ giving the area of a square as contains the points (1,1), (2,4) and (3,9), which etween two quantities. Determine the rate of n of a relationship or from two (x,y) values, terpret the rate of change and initial value of a rms of its graph or a table of values. tween two quantities by analyzing a graph ar or nonlinear). Sketch a graph that exhibits	 them. Reason quantita Construct argume critique of other Model v mathem Use app strategia Attend to I Look for of struct Look for 	ense of ns and re in solving abstractly and atively ct viable nts and the reasoning s. with natics. propriate tools cally. to precision. and make use ure. and express ty in repeated

ESSENTIAL QUESTIONS	VOCABULARY	ASSESSMENT
 How do you define, evaluate, and compare functions? How do you use functions to model relationships between quantities? How do you determine the steepness or rate of change of a linear representation? How do you show linear representations numerically in tables, graphically, and algebraically (equations)? 	 function input output ordered pair rate of change slope slope-intercept non-linear function relations 	Formative:•Journals/logs•KWL chart•At the bell activities•Question and answer•Thumbs up/thumbs down•Individual white boards/Promethean Board ActiVotes•Individual white boards/Promethean Board ActiVotes•Homework•Quizzes•Constructed response/open-ended problem solving•Performance tasks•Exit slipsSummative:•Benchmark assessments•Performance based assessments•Quizzes o Tests•Constructed response/open -ended problem solving•Performance tasks•Performance tasks•Performance tasks•Performance tasks•Project o Spiral Review•Studylsland Practice

	PA CORE ASSESSMENT ANCHORS	PA ELIGIBLE CONTENT STANDARDS/ESSENTIAL CONTENT LEARNING ACTIVITIES
	CC.2.2.8.C.1: Define, evaluate, and compare functions.	M08.B-F.1: Analyze and interpret functions.
FUNCTIONS	 CC.2.2.8.C.1: Define, evaluate, and compare functions. Essential Skills and Understanding Ability to determine whether a relation is a function. Ability to recognize functional relationships and apply the following: Function Tables Vertical Line Test Domain/Input/Independent (x-coordinate) Range/Output/Dependent (y-coordinate) Ability to compare properties-constant rate of range/slope, increasing, decreasing, y-intercept, parallel lines, slopes of horizontal/vertical lines. Ability to calculate slope/rate of change of a line graphically from a table or verbal description. Ability to determine y-intercept from table, equation, graph, or verbal description. Ability to distinguish between linear and non-linear functions. Ability to identify and define independent variables and dependent variables in equations that represent authentic scenarios. CC.2.2.8.C.2: Use concepts of functions to model relationships between quantities. Essential Skills and Understanding Ability to calculate and interpret constant rate of change/slope from a scenario, table, graph, or two points. Ability to calculate and interpret initial value (y- intercept) from a scenario, graph, or table. Ability to distinguish rate of change within an interval of a function. Ability to distinguish rate of change within an interval of a function. Ability to sketch a graph given algebraic context or a scenario (slope and initial value). 	 M08.B-F.1: Analyze and interpret functions. M08.B-F.1.1.1 Determine whether a relation is a function. M08.B-F.1.1.2 Compare properties of two functions, each represented in a different way (i.e., algebraically, graphically, numerically in tables, or by verbal descriptions). M08.B-F.1.1.3 Interpret the equation y = mx + b as defining a linear function whose graph is a straight line; give examples of functions that are not linear. M08.B-F.2.1.1 Construct a function to model relationships between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x,y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models and in terms of its graph or a table of values. M08.B-F.2.1.2 Describe quantitatively the functional relationship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch or determine a graph that exhibits the qualitative features of a function that has been described verbally.
	Ability to create a plausible story given a graph.	

	DIFFERENTIATION A Teacher directed differentiated instructional projects and		
ENRICHMENT:	 Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student 	REMEDIATION:	 Pearson Successnet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments Chunking of content, assignment and/or assessments One-on-one re-teaching Volunteer/peer tutoring Accommodations based on IEP and/or need ELL student(or based on student need) additional support Provide specific examples Simplified language in word problems Visuals Flashcards Multiple-meaning words Bilingual dictionary/picture dictionary

- Pre-Algebra, Pearson Education: Unit 8 ٠ Algebra I, Pearson Education: Unit 1, 2, 3 Studylsland, Ck12Math, other resources below: Functions PDE SAS portal: http://www.pdesas.org Thinking Maps ٠ Graphing calculator Exit Tickets • Adaptions checklist . ELL Instructional Strategies for Math ٠ ESL Handbook Click on "Academic Resources" from PMSD website 0 Click on "ESL" on left side of tool bar. 0 Click on the link to the PMSD ESEL Handbook 0 Scroll through to page 44 in the appendices. 0 Teacher generated/differentiated instruction resources and activities ٠ Grade 8 released state sample questions ٠ Grade 8 generated sample questions ٠ Promethean Flipcharts/ActiVotes ٠ Math flipcharts • Math Internet Resources from PMSD Resource Page ٠ StudyIsland • http://www.khanacademy.org/ . Thinkfinity website: <u>http://www.thinkfinity.org/home</u> ٠ IXL Website: http://www.IXL.com/math/ . United Streaming: http://streaming.discoveryeducation.com/index.cfm • http://edhelper.com/place_value.html . http://illuminations.nctm.org ٠ http://insidemathematics.org . www.teachingchannel.org ٠ http://illustrativemathematics.org/standards/k8 • http://wiki.warren.kyschools.us/aroups/wcpscommoncorestandards/ • www.teachingchannel.org ٠ http://www.learnzillion.com ٠ http://www.teacherspayteachers.com •
 - <u>flexmath.ck12.org/</u>

RESOURCES

ACCELERATED MATH GRADE 7: 180 Day Course	STATE STANDARD AREA/UNIT:	Geometry: Geometry	TIME FRAME		Ongoing
 and areas from a scale d 7.G.2 Draw (freehand, w conditions. Focus on cor conditions determine a u 7.G.3 Describe the two-d sections of right rectangu Solve real-life and mathematical 	eometrical figures and describe to olving scale drawings of geometric rawing and reproducing a scale ith ruler and protractor, and with instructing triangles from three me nique triangle, more than one tri dimensional figures that result from and right rectangular problems involving angle meas	tric figures, including computing actual lengths drawing at a different scale. technology) geometric shapes with given easures of angles or sides, noticing when the angle, or no triangle. m slicing three-dimensional figures, as in plane pyramids. ure, area, surface area, and volume.	 MATHEMATICAL PRACT 1. Make sense of problems and persevere in so them. 2. Reason abstract quantitatively 3. Construct viab arguments and the reasoning of the		e of and in solving ostractly and vely viable s and critique ing of others.
 give an informal derivation 7.G.5 Use facts about supproblem to write and solv 7.G.6 Solve real-world and 	on of the relationship between th oplementary, complementary, v re simple equations for an unkno nd mathematical problems involv	 4. If the contract of a circle and use them to solve problems; to between the circumference and area of a circle. b) between the circumference and area of a circle. b) between the circumference and area of a circle. c) between the circumference and area of a circle. b) between the circumference and area of a circle. c) between the circumference and area of a circle. b) between the circumference and area of a circle. c) between the circumference and area of a circle. b) between the circumference and area of a circle. c) between the circumference and area of a circle. c) between the circumference and area of a circle. c) between the circumference and area of a circle. c) between the circumference and area of a circle. c) between the circumference and area of two-fit trianales, and dilaterals, polyaops, cubes, and right prisms. 	mathema Use appro strategica Attend to Look for ar	ematics. ppropriate tools egically. Id to precision. for and make use	
 8.G.2 Understand that a from the first by a sequend describe a sequence that 8.G.3 Describe the effect using coordinates. 8.G.4 Understand that a from the first by a sequence 	two-dimensional figure is congru ice of rotations, reflections, and t it exhibits the congruence betwe t of dilations, translations, rotation two-dimensional figure is similar t	ns, and reflections on two-dimensional figures to another if the second can be obtained lations, and dilations; given two similar two-	d of structure. 8. Look for and expl regularity in repeared reasoning.		nd express n repeated
 8.G.7 Apply the Pythago and mathematical proble 8.G.8 Apply the Pythago 	he Pythagorean Theorem and its rean Theorem to determine unkr ems in two and three dimensions rean Theorem to find the distanc	nown side lengths in right triangles in real-world ce between two points in a coordinate system.			
 Solve real-world and mathematic 8.G.9 Know the formulas world and mathematical 	for the volumes of cones, cylinde	f cylinders, cones, and spheres. ers, and spheres and use them to solve real-			

ESSENTIAL QUESTIONS
 How do you draw and describe geometrical figures? How do you describe the relationships between geometrical figures? How do you use facts about supplementary, complementary, vertical, and adjacent angles to write and solve simple equations for an unknown angle in a figure? How do you solve real-life and mathematical problems involving angle measure, area, surface area, and volume? How do you use congruence and similarity with physical models or transformations? How do you solve real-world and mathematical problems involving volume of cylinders, cones and spheres?

	PA CORE ASSESSMENT ANCHORS	PA ELIGIBLE CONTENT STANDARDS/ESSENTIAL CONTENT LEARNING ACTIVITIES
	CC.2.3.7.A.2: Visualize and represent geometric figures and describe the relationships between them.	M07.C-G.1: Demonstrate an understanding of geometric figures and their properties.
	 Ability to describe and identify ratios and proportions. Ability to reproduce scale drawing at a different scale. Ability to draw and describe geometrical figures. Ability to use and apply the triangle inequality theorem. Ability to build on prior knowledge with 2-dimensional figures and 3-dimensional figures. Ability to differentiate between the characteristics of right rectangular prisms and right rectangular prisms and right rectangular prisms and right rectangular prisms and right rectangular prisms 	 M07.C-G.1.1.1 Solve problems involving scale drawings of geometric figures, including finding length and area. M07.C-G.1.1.2 Identify or describe the properties of all types of triangles based on angle and side measures. M07.C-G.1.1.3 Use and apply the triangle inequality theorem. M07.C-G.1.1.4 Describe the two-dimensional figures that result from slicing three-dimensional figures.
METRY	 CC.2.3.7.A.1: Solve real-world and mathematical problems involving angle measure, area, surface area, circumference, and volume. Essential Skills and Understanding Ability to identify and apply the vocabulary for a circle – radius, diameter, chord, circumference, center pi (π) ≈ 3.14159 and ²²/₇. Ability to explore the relationship between the angles of intersecting lines and figures. Ability to identify and use properties of supplementary, complementary and adjacent angles in a multistep problem to write and solve simple equations for an unknown angle in a figure. Ability to find the area and circumference of a circle and to solve problems involving area and circumference of a circle(s). Ability to solve real-world and mathematical problems involving area, volume, and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. 	 M07.C-G.2: Solve real-world and mathematical problems involving angle measure, circumference, area, surface area, and volume. M07.C-G.2.1.1 Identify and use properties of supplementary, complementary and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure. M07.C-G.2.1.2 Identify and use properties of angles formed when two parallel lines are cut by a transversal (e.g., angles may include alternate interior, alternate exterior, vertical, corresponding). M07.C-G.2.2.1 Find the area and circumference of a circle. Solve problems involving area and circumference of a circle(s). M07.C-G.2.2.2 Solve real-world and mathematical problems involving area, volume, and surface area to two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes and right prisms.

CC.2.3.8.A.2: Understand and apply congruence, similarity, and geometric transformations using various tools.

Essential Skills and Understanding

- Ability to Identify and apply properties of rotations, reflections, and translations. Example: Angle measures are preserved in rotations, reflections, and translations.
- Ability to describe a sequence of transformations that exhibits the congruence between them given two congruent figures.
- Ability to describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.
- Ability to describe a sequence of transformations that exhibits the similarity between them given two similar two-dimensional figures.

CC.2.3.8.A.3: Understand and apply the Pythagorean Theorem to solve problems.

Essential Skills and Understanding

- Ability to apply the converse of the Pythagorean theorem to show a triangle is a right triangle.
- Ability to apply the Pythagorean theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions.
- Ability to apply the Pythagorean theorem to find the distance between two points in a coordinate system.

CC.2.3.8.A.1: Apply the concepts of volume of cylinders, cones, and spheres to solve real-world and mathematical problems.

Essential Skills and Understanding

• Ability to apply formulas for the volumes of cones, cylinders, and spheres to solve real-world and mathematical problems. Formulas will be provided.

M08.C-G.1: Demonstrate an understanding of geometric transformations.

M08.C-G.1.1.1

• Identify and apply properties of rotations, reflections, and translations. Example: Angle measures are preserved in rotations, reflections, and translations.

M08.C-G.1.1.2

• Given two congruent figures, describe a sequence of transformations that exhibits the congruence between them.

M08.C-G.1.1.3

• Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.

M08.C-G.1.1.4

• Given two similar two-dimensional figures, describe a sequence of transformations that exhibits the similarity between them.

M08.C-G.2: Understand and apply the Pythagorean Theorem.

M08.C-G.2.1.1

• Apply the converse of the Pythagorean theorem to show a triangle is a right triangle.

M08.C-G.2.1.2

 Apply the Pythagorean theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions. (Figures provided for problems in three dimensions will be consistent with Eligible Content in grade 8 and below.)

M08.C-G.2.1.3

• Apply the Pythagorean theorem to find the distance between two points in a coordinate system.

M08.C-G.3: Solve real-world and mathematical problems involving volume.

M08.C-G.3.1.1

• Apply formulas for the volumes of cones, cylinders, and spheres to solve real-world and mathematical problems. **Formulas will be provided.**

	DIFFERENTIATION ACTIVITIES: Teacher directed differentiated instructional projects and activities are ongoing and based on student need.						
ENRICHMENT:	 Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student 	REMEDIATION:	 Pearson Successnet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments One-on-one re-teaching Volunteer/peer tutoring Accommodations based on IEP and/or need ELL student(or based on student need) additional support <u>Provide specific examples</u> <u>Use of Manipulatives</u> <u>Simplified language in word problems</u> <u>Visuals</u> <u>Flashcards</u> <u>Multiple-meaning words</u> <u>Bilingual dictionary/picture dictionary</u> 				

- Course 2, Pearson Education: Unit 7, 8
- Pre-Algebra, Pearson Education: Unit 9, 10, 11
- StudyIsland, Ck12Math, other resources below: Geometry
- PDE SAS portal: <u>http://www.pdesas.org</u>
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - Click on the link to the PMSD ESEL Handbook
 - Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Grade 8 released state sample questions
- Grade 8 generated sample questions
- Promethean Flipcharts/ActiVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- <u>http://www.khanacademy.org/</u>
- Thinkfinity website: <u>http://www.thinkfinity.org/home</u>
- IXL Website: http://www.IXL.com/math/
- United Streaming: <u>http://streaming.discoveryeducation.com/index.cfm</u>
- <u>http://edhelper.com/place_value.html</u>
- http://illuminations.nctm.org
- <u>http://insidemathematics.org</u>
- <u>www.teachingchannel.org</u>
- <u>http://illustrativemathematics.org/standards/k8</u>
- <u>http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/</u>
- <u>www.teachingchannel.org</u>
- http://www.learnzillion.com
- <u>http://www.teacherspayteachers.com</u>
- <u>flexmath.ck12.org/</u>

ACCELERATED MATH GRADE 7: 180 Day Course	STATE STANDARD	AREA/UNIT:	Numbers and Operatio The Number System	ns: TIA	NE FRAME:	Ongoing	
 NATIONAL COMMON CORE STANDARDS: Know that there are numbers that are not rational, and approximate them by rational numbers. 8.NS.1 Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which eventually into a rational number. 8.NS.2 Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., π²). For example, by truncating the decimal expansion of √2 show that √2 is between 1 and 2, then between 1.4 and 1.5, and explain how to continue on to get better approximations. 				1. 2. 3. 4. 5. 6. 7.	 MATHEMATICAL PRACTICES: Make sense of problems and persevere in solving them. Reason abstractly and quantitatively Construct viable arguments and critique the reasoning of others. Model with mathematics. Use appropriate tools strategically. Attend to precision. Look for and make use of structure. Look for and express regularity in repeated reasoning. 		
ESSENTIAL QUESTIONS VOCABULARY • How do you distinguish between rational and irrational numbers using their properties? • rational numbers • How do you identify and provide examples of rational versus irrational numbers of the real number system? • radical • How do you estimate irrational numbers • repeating decimals • How do you estimate irrational numbers • repeating decimals		Eorm(• • • • • • • • • • • • •	ative: Journals/log KWL chart At the bell of Question ar Thumbs up/ Individual w Board Activ Homework Quizzes	activities nd answer thumbs down rhite boards/Promethean rotes d response/open-ended ving			

ESSENTIAL QUESTIONS	VOCABULARY	ASSESSMENT
		Summative: • Benchmark assessments • Performance based assessments • Quizzes • Tests • Constructed response/open- ended problem solving • Performance tasks • Project • Spiral Review • Studylsland Practice

	PA CORE ASSESSMENT ANCHORS	PA ELIGIBLE CONTENT STANDARDS/ESSENTIAL CONTENT LEARNING ACTIVITIES
UNIT OF INSTRUCTION: THE NUMBER SYSTEM	CC.2.1.8.E.1: Distinguish between rational and irrational numbers using their properties.	M08.A-N.1: Demonstrate an understanding of rational and irrational numbers. M08.A-N.1.1.1
	 Essential Skills and Understanding Knowledge of differences between rational and irrational. Knowledge of definition and description of rational and irrational. Ability to show that the decimal expansion terminates or repeats (limit repeating decimals to thousandths). Ability to covert a terminating or repeating decimal to a rational number (limit repeating decimals to thousandths). Ability to identify and provide examples of rational versus irrational numbers, of the real number system. 	 Determine whether a number is rational or irrational. For rational numbers, show that the decimal expansion terminates or repeats (limit repeating decimals to thousandths). M08.A-N.1.1.2 Convert a terminating or repeating decimal to a rational number (limit repeating decimals to thousandth). M08.A-N.1.1.3
	 CC.2.1.8.E.4: Estimate irrational numbers by comparing them to rational numbers. Essential Skills and Understanding Ability to estimate the value of irrational numbers without a calculator. Ability to use rational approximations of irrational numbers to compare and order irrational numbers. Ability to use a number line that specifies in tenths and hundredths the value between two whole numbers. Ability to use a number line that extends indefinitely, such as π. 	 Estimate the value of irrational numbers without a calculator (limit whole number radicand to less than 144). M08.A-N.1.1.4 Use rational approximations of irrational numbers to compare and order irrational numbers. M08.A-N.1.1.5 Locate/identify rational and irrational numbers at their approximate locations on a number line.

	DIFFERENTIATION ACTIVITIES: Teacher directed differentiated instructional projects and activities are ongoing and based on student need.							
ENRICHMENT:	 Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student 	REMEDIATION:	 Pearson Successnet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments Chunking of content, assignment and/or assessments One-on-one re-teaching Volunteer/peer tutoring Accommodations based on IEP and/or need ELL student (or based on student need) additional support Provide specific examples Use of Manipulatives Simplified language in word problems Visuals Flashcards Multiple-meaning words Bilingual dictionary/picture dictionary 					

- Pre-Algebra, Pearson Education: Unit 3, 4, 5, 11
- Grade 7 Units: Numbers and Operations: The Number System and Ratios and Proportional Relationships, as needed for review of new concepts
- Studylsland, Ck12Math, other resources below: The Number System
- PDE SAS portal: <u>http://www.pdesas.org</u>
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - o Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - o Click on the link to the PMSD ESEL Handbook
 - Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Grade 8 released state sample questions
- Grade 8 generated sample questions
- Promethean Flipcharts/ActiVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- <u>http://www.khanacademy.org/</u>
- Thinkfinity website: <u>http://www.thinkfinity.org/home</u>
- IXL Website: http://www.IXL.com/math/
- United Streaming: <u>http://streaming.discoveryeducation.com/index.cfm</u>
- <u>http://edhelper.com/place_value.html</u>
- <u>http://illuminations.nctm.org</u>
- <u>http://insidemathematics.org</u>
- <u>www.teachingchannel.org</u>
- <u>http://illustrativemathematics.org/standards/k8</u>
- <u>http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/</u>
- <u>www.teachingchannel.org</u>
- http://www.learnzillion.com
- <u>http://www.teacherspayteachers.com</u>
- <u>flexmath.ck12.org/</u>

ACCELERATED MATH GRADE 7: 180 Day Course	STATE STANDARD AREA/UNIT:	Measurement, Data and Probability: Statistics and Probability	TIM	E FRAME:	Ongoing		
NATIONAL COMMON CORE STAN	MATHE	MATICAL PRA	CTICES:				
Use random sampling to draw in	1.	Make sense of	of problems				
• 7.SP.1 Understand that s		and persever	re in solving				
sample of the populatior		them.	0				
		hat random sampling tends to produce	2	Reason abstr	actly and		
	۷.						
	ind support valid inferences.		•	quantitatively			
		es about a population with an unknown	3.	Construct vic			
		simulated samples) of the same size to		arguments a			
gauge the variation in es	timates or predictions. For exam	nple, estimate the mean word length in a	the reasoning of others.				
book by randomly sampl	ing words from the book; predic	t the winner of a school election based on	4.	Model with m	nathematics.		
randomly sampled surve	y data. Gauge how far off the e	estimate or prediction miaht be.	5.	Use appropri	ate tools		
	,			strategically.			
Draw informal comparative infer	ences about two populations.		6	Attend to pre	cision		
 7.SP.3 Informally assess the 	ne degree of visual overlap of tw	vo numerical data distributions with similar		Look for and			
	C	s by expressing it as a multiple of a measure	7.		make use of		
		the basketball team is 10 cm greater than	-	structure.			
			8.	Look for and	•		
o		vice the variability (mean absolute		regularity in r	epeated		
	n; on a dot plot, the separation b	between the two distributions of heights is		reasoning.			
noticeable.		-					
 7.SP.4 Use measures of c 							
		ulations. For example, decide whether the					
words in a chapter of seventh-grade science book are generally longer than the words in a chapter of a fourth-grade science book.							
of a room-grade science book.							
Investigate chance processes a	Investigate chance processes and develop, use, and evaluate probability models.						
		t is a number between 0 and 1 that					
		umbers indicate greater likelihood. A					
•	a a						
	<i>i i</i>	ty around ½ indicates and event that is					
neither unlikely nor likely,	and a probability near 1 indicate	es a likely event.					
Investigate nations of genericity	n in hiveriate data						
Investigate patterns of association							
	• •	neasurement data to investigate patterns					
		s such as clustering, outliers, positive or					
negative association, line	ear association, and nonlinear as	ssociation.					
 8.SP.2 Know that straight 	8.SP.2 Know that straight lines are widely used to model relationships between two quantitative						
variables. For scatter plots that suggest a linear association, informally fit a straight line, and							
informally assess the model fit by judging the closeness of the data points to the line.							
 8.SP.3 Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. For example, in a linear model for a biology experiment, 							
		÷					
interpret a slope of 1.5 Cl	nnii as meaning that an additio	nal hour of sunlight each day is associated					

with an addition 1/5 cm in mature plant height.

• **8.SP.4** (Optional) Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. For example, collect data from students in your class on whether or not they have a curfew on school nights and whether or not they have assigned chores at home. Is there evidence that those who have a curfew also tend to have chores?

	PA CORE ASSESSMENT ANCHORS	PA ELIGIBLE CONTENT STANDARDS/ESSENTIAL CONTENT LEARNING ACTIVITIES
	CC.2.4.7.B.1: Draw inferences about populations based on random sampling concepts.	M07.D-S.1.: Use random sampling to draw inferences about a population.
UNIT OF INSTRUCTION: STATISTICS AND PROBABILITY	 Essential Skills and Understanding Ability to describe and identify population, samples of a population, random sampling, validity, reliability, invalid, inferences. Ability to use data from a random sample to draw inferences about a population with an unknown characteristic of interest. CC.2.4.7.B.2: Draw informal comparative inferences about two populations. Essential Skills and Understanding Ability to describe and identify deviation, standard deviation, absolute deviation, measures of central tendency, measures of variability. Ability to build on prior experience with dot plots and to make inferences from the data. Ability to use statistical findings to draw inference about populations. CC.2.4.7.B.3: Investigate chance processes and develop, use, and evaluate probability models. Essential Skills and Understanding Ability to devise models where outcomes are equally likely versus not equally likely. Ability to describe and identify possibility versus probability. Ability to describe and identify possibility versus probability. Ability to describe and identify possibility versus probability. Ability to describe and identify possibility versus probability. Ability to compare simple events with compound events. Ability to find probabilities of independent compound events. Ability to use models and simulate a variety of events. 	 M07.D-S.1.1.1 Determine whether a sample is a random sample given a real-world situation. M07.D-S.1.1.2 Use data from a random sample to draw inferences about a population with an unknown characteristic of interest. M07.D-S.2: Draw comparative inferences about populations. M07.D-S.2: Draw comparative inferences about populations. M07.D-S.2: Draw comparative inferences about populations. M07.D-S.2: Investigate chance processes and develop, use, and evaluate probability models. M07.D-S.3: Investigate chance processes and develop, use, and evaluate probability models. M07.D-S.3.1.1 Predict or determine whether some outcomes are certain, more likely, less likely, equally likely, or impossible (i.e., a probability near 0 indicates an unlikely event, a probability around ½ indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event). M07.D-S.3.2.1 Determine the probability of a chance event given relative frequency. Predict the approximate relative frequency given the probability. M07.D-S.3.2.2 Find the probability of a simple event, including the probability of a simple event not occurring. M07.D-S.3.2.3 Find probabilities of independent compound events using organized lists, tables, tree diagrams, and simulation.

CC.2.4.8.B.1: Analyze and/or interpret bivariate data displayed in	M08.D-S.1.: Investigate patterns of association in bivariate data.
 multiple representations. Essential Skills and Understanding Ability to integrate technology and relate data scenarios to authentic real life situations. Ability to keep paired data organized in relation to one another within two sets of quantities. Ability to describe patterns such as clustering, outliers, positive or negative correlation, linear association, and nonlinear association. Ability to identify a line of best fit by judging the closeness of the data points to the line. Ability to use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. 	 M08.D-S.1.1.1 Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative correlation, linear association, and nonlinear association. M08.D-S.1.1.2 For scatter plots that suggest a linear association, identify of line of best fit by judging the closeness of the data points to the line. M08.D-S.1.1.3 Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. M08.D-S.1.2.1 (Optional)
 CC.2.4.8.B.2: Understand that patterns of association can be seen in bivariate data utilizing frequencies. (Optional) Essential Skills and Understanding Ability to use the equation of a linear model to solve problems in the context of data by using the slope and intercept. Ability to construct and interpret a two-way table summarizing data with two categorical variables collected. Ability to use relative frequencies calculated for rows or columns to describe possible associations between the two variables. 	 Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible associations between the tw variables.

	DIFFERENTIATION ACTIVITIES: Teacher directed differentiated instructional projects and activities are ongoing and based on student need.						
ENRICHMENT:	 Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student 	REMEDIATION:	 Pearson Successnet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Ck12Math Web-based Math Resources Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments Chunking of content, assignment and/or assessments One-on-one re-teaching Volunteer/peer tutoring Accommodations based on IEP and/or need ELL student(or based on student need) additional support <u>Provide specific examples</u> <u>Use of Manipulatives</u> <u>Simplified language in word problems</u> <u>Visuals</u> <u>Flashcards</u> <u>Multiple-meaning words</u> <u>Bilingual dictionary/picture dictionary</u> 				

- Pre-Algebra, Pearson Education: Unit 6, 8, 12 (Optional) ٠ Course 2, Pearson Education: Unit 7, 8 Studylsland, Ck12Math, other resources below: Statistics and Probability • PDE SAS portal: http://www.pdesas.org Thinking Maps ٠ Graphing calculator Exit Tickets • Adaptions checklist . ELL Instructional Strategies for Math ٠ ESL Handbook Click on "Academic Resources" from PMSD website 0 Click on "FSI" on left side of tool bar. 0 Click on the link to the PMSD ESEL Handbook 0 Scroll through to page 44 in the appendices. 0 Teacher generated/differentiated instruction resources and activities ٠ Grade 8 released state sample questions . Grade 8 generated sample guestions RESOURCES ٠ Promethean Flipcharts/ActiVotes • Math flipcharts • Math Internet Resources from PMSD Resource Page ٠ StudvIsland • http://www.khanacademy.org/ • Thinkfinity website: <u>http://www.thinkfinity.org/home</u> ٠ IXL Website: http://www.IXL.com/math/ . United Streaming: http://streaming.discoveryeducation.com/index.cfm ٠ http://edhelper.com/place_value.html . http://illuminations.nctm.org • http://insidemathematics.org ٠ www.teachingchannel.org • www.Learnzillion.com • http://illustrativemathematics.org/standards/k8 • http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/ . www.teachingchannel.org ٠ http://www.learnzillion.com •
 - <u>http://www.teacherspayteachers.com</u>
 - <u>flexmath.ck12.org/</u>